




Mathematics Multiplication Calculations Policy 2022- 2023

'Working together to achieve success'

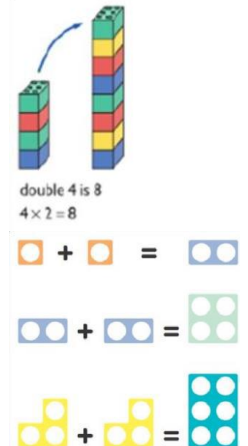
	Concrete	Pictorial	Abstract
Reception Multiplication			
	<p>Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities involving equal sets or groups using a wide variety of equipment, e.g. small world play, role play, counters, cubes etc. They develop ways of recording calculations using pictures, etc.</p> <p>Children may also investigate putting items into resources such as egg boxes, ice cube trays and baking tins which are arrays.</p> 	<p>Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities using a wide variety of equipment, including small world play, role play, counters, cubes etc.</p>  <p>A child's jotting showing the fingers on each hand as a double.</p> <p>They may develop ways of recording calculations using pictures, etc.</p>  <p>A child's jotting showing double three as three cookies on each plate.</p>	



Year 1 Multiplication

Doubling

Use practical activities with manipulatives including cubes and Numicon to demonstrate doubling

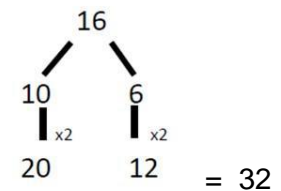


Draw pictures to show to double numbers

Double 4 is 8



Partition a number and then double each part before recombining it back together.

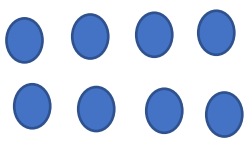


Counting in multiples

Count the groups as children are skip counting children may use their fingers as they are skip counting.


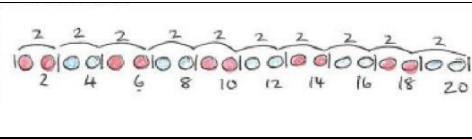


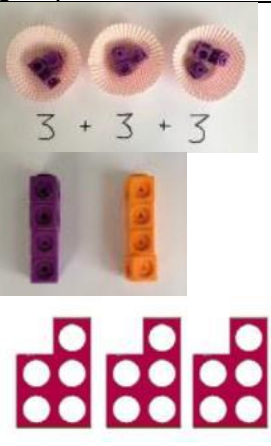




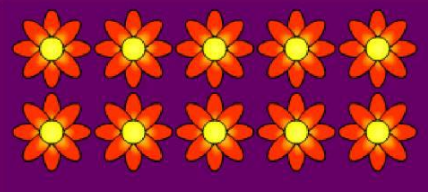


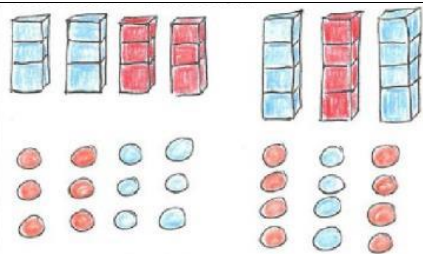
Children make representations to show counting in multiples.



Count in multiples of a number aloud. Write sequences with multiples of numbers.

- 2, 4, 6, 8, 10
- 5, 10, 15, 20, 25

			
<p>Making equal groups and counting the total</p>	 <p>Use manipulatives to create equal groups.</p>	<p>Draw  to show $2 \times 3 = 6$</p> <p>Draw and make representations</p>	<p>$2 \times 4 = 8$</p>
<p>Repeated Addition</p>	 <p>Use different objects to add equal groups.</p>	<p>Use pictorial including number lines to solve problems</p> <p>There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p>   	<p>Write addition sentences to describe objects and pictures</p>  <p>$2 + 2 + 2 + 2 + 2 = 10$</p>
<p>Understanding arrays</p>	<p>Use objects laid out in arrays to find the answers to 2 lots of 5, 3 lots of 2...</p> 	<p>Draw representations to show arrays to show understanding</p>	<p>$3 \times 2 = 6$ How many eggs would we need to fill the egg box? How do you know? $2 \times 5 = 10$</p>



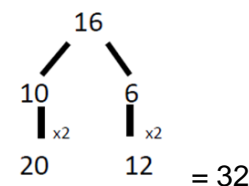
Year 2 Multiplication

Doubling

Model doubling using dienes and place value counters

Draw pictures and representations to show how to double numbers.

Partition a number and then double each part before recombining it back together.



Counting in multiples of 2, 3, 5, 10 from 0

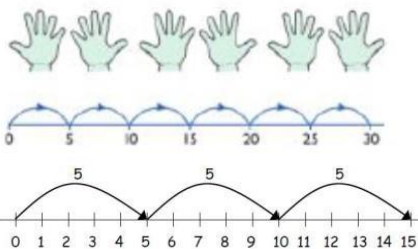
Count the groups as the children are skip counting, children may use their fingers

Number lines, counting sticks and bar models should be used to show representations of counting in multiples

Count in multiples of a number aloud. Write number sequences with multiples of numbers

Use bar models

$$5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$$



0,2,4,6,8,10

0,3,6,9,13

0, 5, 10, 25, 20

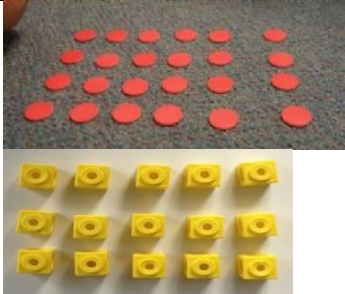
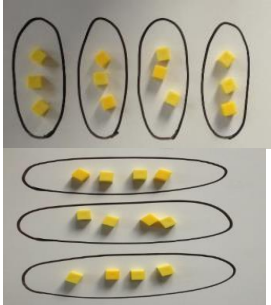
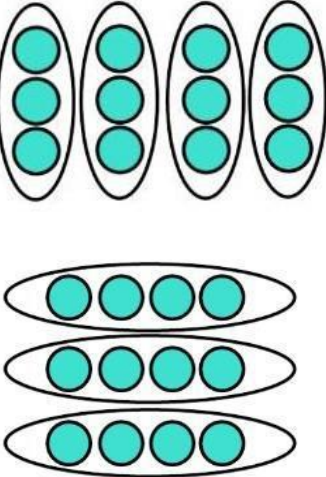


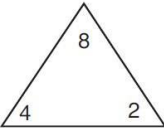
Multiplication is commutative

Create arrays using counters, cubes and numicon

Use representations of arrays to show different calculations and explore commutativity.

$$12 = 3 \times 4$$

$$12 = 4 \times 3$$

	 <p>Children should know the array can show different equations</p> 		<p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$
<p>Using the inverse</p> <p>This is taught alongside division</p>		 $\square \times \square = \square$ $\square \times \square = \square$ $\square \div \square = \square$ $\square \div \square = \square$	$2 \times 4 = 8$ $4 \times 2 = 8$ $8 \div 2 = 4$ $8 \div 4 = 2$ $8 = 2 \times 4$ $8 = 4 \times 2$ $2 = 8 \div 4$ $4 = 8 \div 2$
<p>Year 3 Multiplication</p>			
<p>Use arrays</p>	<p>use apparatus to make the array</p>	<p>Children should continue to utilise multiplication as repeated addition linked to arrays (as this knowledge will support with the development of the grid method) and use jottings to support</p>	$4 \times 7 = 28$ $7 \times 4 = 28$

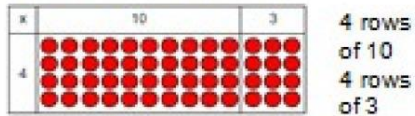
their calculation. These should be supported by the use of crosses on squared paper, e.g.
 $4 \times 7 =$

X	X	X	X	X	X	X
X	X	X	X	X	X	X
X	X	X	X	X	X	X
X	X	X	X	X	X	X

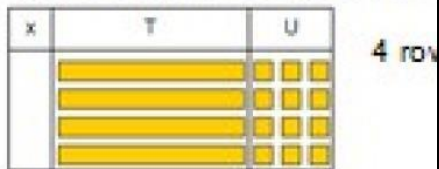
$$4 \times 7 = 7 + 7 + 7 + 7 = 28$$

Grid Method

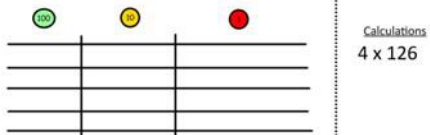
Show the array and introduce the grid method



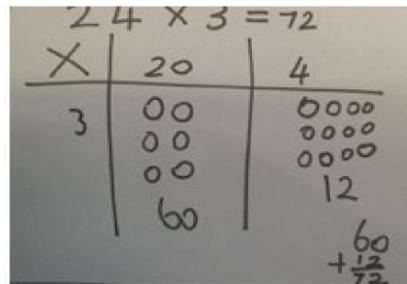
Show it as base 10



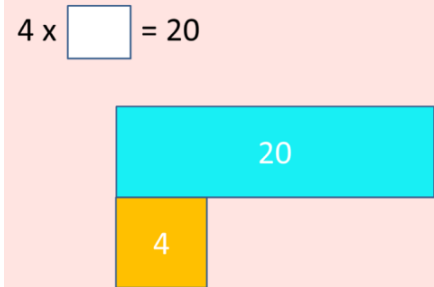
Use place value counters within the grid



Children to represent their work using place value counters in a way they understand.

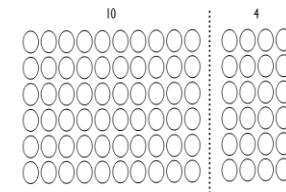


Bar models are used to show missing numbers



TU x U (Short multiplication – multiplication by a single digit)

As they progress to multiplying a two-digit number by a single digit number, children should use their knowledge of partitioning two digit numbers into tens and units/ones to help them. For example, when calculating 14×6 , children should set out the array, then partition the array so that one array has ten columns and the other four.



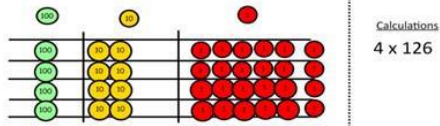
Partitioning in this way, allows children to identify that the first array shows 10×6 and the second array shows 4×6 . These can then be added to calculate the answer:

$$(6 \times 10) + (6 \times 4)$$

$$= 60 + 24$$

$$= 84$$

NB There is no requirement for children to record in this way, but it could be used as a jotting to support development if needed.



Calculations
4 x 126

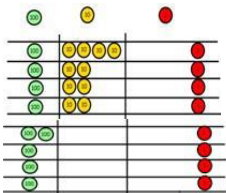
Add up each column starting with

Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

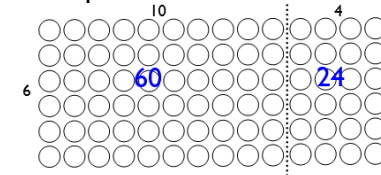
x	30	5
7	210	35

$$210 + 35 = 245$$

the ones and exchanging where needed.



This method is the precursor step to the grid method. Using a two-digit by single digit array, they can partition as above, identifying the number of rows and the number of columns each side of the partition line.

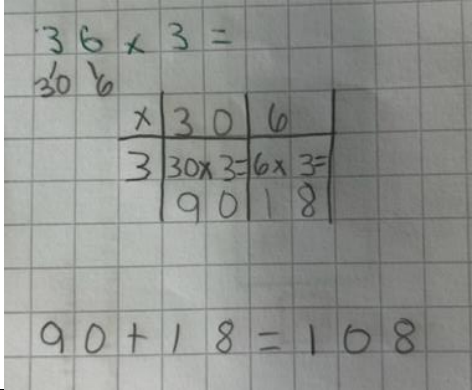


By placing a box around the array, as in the example below, and by removing the array, the grid method can be seen.

x	10	4
6	60	24

It is really important that children are confident with representing multiplication statements as arrays and understand the rows and columns structure before they develop the written method of recording.

From this, children can use the grid method to calculate two-digit by one-digit multiplication calculations, initially with two digit numbers less than 20. Children should be encouraged to set out their addition in a column at the side to ensure the place value is maintained. When children are working with numbers where they can confidently and correctly calculate the addition mentally, they may do so.

			13×8 <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td>x</td><td>10</td><td>3</td></tr> <tr><td>8</td><td>80</td><td>24</td></tr> </table> $+ \begin{array}{r} 80 \\ 24 \\ \hline 104 \end{array}$ <p>When children are ready, they can then progress to using this method with other two-digit numbers.</p> 37×6 <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td>x</td><td>30</td><td>7</td></tr> <tr><td>6</td><td>180</td><td>42</td></tr> </table> $+ \begin{array}{r} 180 \\ 42 \\ \hline 222 \end{array}$ <p>Children should also be using this method to solve problems and multiply numbers in the context of money or measures.</p> 	x	10	3	8	80	24	x	30	7	6	180	42
x	10	3													
8	80	24													
x	30	7													
6	180	42													

Year 4 Multiplication									
Grid method	Manipulatives may be used alongside the grid method	Children to represent their work using place value counters in a way they understand.	<p>Children will move to Y4 using whichever method they were using as they transitioned from Y3. They will further develop their knowledge of the grid method to multiply any two-digit by any single-digit number, e.g.</p> 79×8 <table border="1" style="display: inline-table; margin-right: 20px;"> <tr><td>x</td><td>70</td><td>9</td></tr> <tr><td>8</td><td>560</td><td>72</td></tr> </table> $+ \begin{array}{r} 560 \\ 72 \\ \hline 632 \end{array}$ <p>To support the grid method, children should develop their understanding of place value and facts that are linked to their knowledge of tables. For example, in the calculation above, children</p>	x	70	9	8	560	72
x	70	9							
8	560	72							

should use their knowledge that $7 \times 8 = 56$ to know that $70 \times 8 = 560$.

By the end of the year, they will extend their use of the grid method to be able to multiply three-digit numbers by a single digit number, e.g.

$$\begin{array}{r}
 346 \times 8 \\
 \begin{array}{|c|c|c|c|}
 \hline
 \times & 300 & 40 & 6 \\
 \hline
 8 & 2400 & 320 & 48 \\
 \hline
 \end{array}
 \end{array}
 \qquad
 \begin{array}{r}
 2400 \\
 + 320 \\
 + 48 \\
 \hline
 2768
 \end{array}$$

When children are working with numbers where they can confidently and correctly calculate the addition (or parts of the addition) mentally, they may do so.

Children should also be using this method to solve problems and multiply numbers in the context of money or measures.

Year 5 Multiplication

Grid method continued for 2- and 3-digit numbers by 2-digit numbers

Manipulatives may be used alongside the grid method

Children should continue to use the grid method and extend it to multiplying numbers with up to four digits by a single digit number, e.g.

$$\begin{array}{r}
 4346 \times 8 \\
 \begin{array}{|c|c|c|c|c|}
 \hline
 \times & 4\ 000 & 300 & 40 & 6 \\
 \hline
 8 & 32\ 000 & 2400 & 320 & 48 \\
 \hline
 \end{array}
 \end{array}
 \qquad
 \begin{array}{r}
 32000 \\
 + 2400 \\
 + 320 \\
 + 48 \\
 \hline
 34768
 \end{array}$$

and numbers with up to four digits by a two-digit number, e.g.

$$\begin{array}{r}
 2693 \times 24 \\
 \begin{array}{|c|c|c|c|c|}
 \hline
 \times & 2000 & 600 & 90 & 3 \\
 \hline
 20 & 40000 & 12000 & 1800 & 60 \\
 \hline
 4 & 8000 & 2400 & 360 & 12 \\
 \hline
 \end{array}
 \end{array}
 \qquad
 \begin{array}{r}
 40000 \\
 + 8000 \\
 + 12000 \\
 + 2400 \\
 + 1800 \\
 + 360 \\
 + 60 \\
 + 12 \\
 \hline
 64632
 \end{array}$$

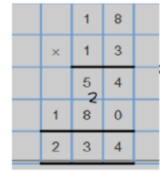
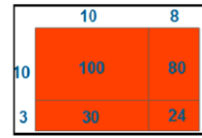
When children are working with numbers where they can confidently and correctly calculate the

			addition (or parts of the addition) mentally, they may do so.																						
Start to then introduce short multiplication	Manipulatives may be still used with the long multiplication method alongside.		<table border="1" style="margin-bottom: 10px;"> <tr><td>x</td><td>300</td><td>20</td><td>7</td></tr> <tr><td>4</td><td>1200</td><td>80</td><td>28</td></tr> </table> $ \begin{array}{r} 327 \\ \times 4 \\ \hline 28 \\ 80 \\ 1200 \\ \hline 1308 \end{array} $ <table border="1" style="margin-bottom: 10px;"> <tr><td>3</td><td>2</td><td>7</td></tr> <tr><td>x</td><td></td><td>4</td></tr> <tr><td>1</td><td>3</td><td>0</td><td>8</td></tr> <tr><td></td><td>1</td><td>2</td><td></td></tr> </table> <p style="font-size: small;">This will lead to a compact method.</p> <p style="text-align: center;">1308</p>	x	300	20	7	4	1200	80	28	3	2	7	x		4	1	3	0	8		1	2	
x	300	20	7																						
4	1200	80	28																						
3	2	7																							
x		4																							
1	3	0	8																						
	1	2																							
Introduce decimal multiplication			$ \begin{array}{r} 4.9 \times 3 \\ \oplus \\ \times 4.09 \\ 3 \quad \boxed{12} \quad \boxed{2.7} \\ \hline 12 \\ + 2.7 \\ \hline 14.7 \quad \square \end{array} $ <p>Use knowledge of place value and multiplication facts to divide related decimal numbers.</p>																						

Year 6 Multiplication

Column multiplication

Manipulatives may be still used with the long multiplication method alongside.



$$\begin{array}{r}
 1234 \\
 \times \quad 16 \\
 \hline
 7404 \\
 12340 \\
 \hline
 19744
 \end{array}$$

Multiplying decimals up to 2 decimal places by a single digit

4.92×3

$$\begin{array}{r}
 \text{⊕} \\
 \times \quad 4 \quad 0.9 \quad 0.02 \\
 3 \quad \boxed{12} \quad \boxed{2.7} \quad \boxed{0.06} \\
 \hline
 12 \\
 + 2.7 \\
 + 0.06 \\
 \hline
 14.76
 \end{array}$$

Moving to

$$\begin{array}{r}
 3.19 \\
 \times 8 \\
 \hline
 25.52
 \end{array}$$

Multiply the decimal by 10, 100 or 1000 to make it a whole then complete the calculation. Once complete divide by the same multiple.

e.g

$$\begin{aligned}
 &3.19 \times 8 \\
 &3.19 \times 100 = 319 \\
 &319 \times 8 = 2,552 \\
 &2,552 \div 100 = 25.52
 \end{aligned}$$

Multiplication

